Problem 1: Let $A$ be an $n \times n$ matrix, and $B$ the matrix obtained from $A$ by multiplying the $i$-th column of $A$ by a number $\alpha$. Show that $\operatorname{det} B=\alpha \operatorname{det} A$.

Problem 2: Let $A$ be an $n \times n$ matrix, and $B$ the matrix obtained from $A$ by adding a multiple of the $j$-th column to the $i$-th column. Show that $\operatorname{det} B=\operatorname{det} A$.

