

Prove that $|\mathbf{v} \times \mathbf{w}|^2 = |\mathbf{v}|^2|\mathbf{w}|^2 - (\mathbf{v} \cdot \mathbf{w})^2$ for any $\mathbf{v}, \mathbf{w} \in \mathbb{R}^3$.